Evidence for prolate structure in light Pb isotopes from in-beam γ-ray spectroscopy of $^{185}$Pb


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For the first time, excited states in $^{185}$Pb have been observed in in-beam γ-ray spectroscopic measurements using the recoil-decay tagging method. The resulting level scheme reveals a strongly coupled yrast band structure that originates from coupling of the $i_{13/2}$ quasineutron to a prolate deformed core. The band is also observed to de-excite via the spherical $α$-decaying 13/2$^+$ isomeric state.

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A considerable body of both theoretical and experimental evidence has been gathered for coexisting configurations possessing different shapes in the very neutron deficient Pb isotopes [1,2]. This phenomenon becomes particularly apparent in Pb isotopes in the vicinity of the $N = 104$ neutron midshell, where the competing deformed structures intrude down to energies close to the spherical ground state. The intruder states have been associated with proton multiparticle-multihole excitations across the closed $Z = 82$ shell [3–5]. This picture is supported by hindrance factors obtained in $α$-decay fine-structure studies [5]. Mean-field calculations suggest that each intruder configuration can be associated with a different shape [7–11]. Together with the spherical ground state, they result in a unique triplet of shape-coexisting 0$^+$ states in $^{186}$Pb [12].

In in-beam γ-ray studies via fusion-evaporation reactions, rotational yrast bands have been observed in even-mass $^{182–189}$Pb nuclei [13–16]. The moments of inertia of these bands resemble those of yrast bands in even-mass Hg isotones and they have been associated with the prolate minimum [1,2]. Candidates for oblate non-yrast bands have also been seen in $^{186}$Pb and $^{188}$Pb [15,16]. Recently, lifetime measurements have provided more information concerning the collectivity and deformation of the yrast bands in $^{186}$Pb and $^{188}$Pb [17,18], but more evidence regarding their shape is still needed.

Information about the shape of the midshell Pb nuclei can be obtained by probing band structures in their neighboring odd-mass nuclei. The coupling of the odd quasiparticle to the even-even core results in a characteristic level pattern, depending on the shape of the core nucleus. So far, in odd-A Pb isotopes of $A > 189$, yrast structures have been associated with weak coupling of an $i_{13/2}$ neutron hole to the yrast states of the neighboring nearly spherical even-A nucleus [19–25]. In $^{189}$Pb, the yrast states are associated with the spherical shape, but strong mixing with the prolate states is indicated by $E0$ contributions observed in transitions between levels of the same spin and parity. In the same nucleus, a non-yrast band structure has been observed in the decay of a high-spin isomeric state, and the $i_{13/2}$ quasineutron to the shape-coexisting prolate core [19]. For $^{187}$Pb, two alternative explanations were given by Baxter et al., who associated the observed yrast states with the weak coupling of the $i_{13/2}$ quasineutron to the spherical core or with the favored signature states resulting from the strong coupling of this neutron to the shape-coexisting prolate core. In the study of $^{187}$Bi and $^{189}$Bi isotopes, the $1^+_2$ orbitals have been observed [27]. Thus, the investigation of $^{185}$Pb can provide important direct evidence on nuclear shape in the Pb isotopes around the $N = 104$ neutron midshell through the character of particle-core coupling [28].

Fusion-evaporation reactions can be employed to populate excited states in midshell Pb nuclei. However, due to the small production cross sections and other competing reaction channels, especially fission, in-beam spectroscopic studies are only possible when employing the recoil-decay tagging.
(RDT) technique [29,30]. In the present work, an in-beam γ-ray spectroscopic study of $^{185}$Pb has been carried out by employing the gas-filled recoil separator RITU [31] and the associated detector systems dedicated to RDT experiments at the Accelerator Laboratory of the University of Jyväskylä (JYFL), Finland.

Data from two different in-beam experiments were collected. The $^{82}$Kr + $^{106}$Pd and $^{83}$Kr + $^{104}$Pd reactions were used with $^{32}$Kr and $^{83}$Kr beams of 367 and 362 MeV, respectively, extracted from the JYFL cyclotron. The irradiation time was 6 days in both experiments. The first experiment was optimized for $^{185}$Pb produced via the $3n$-fusion evaporation channel, whereas in the second experiment (dedicated to a study of $^{184}$Pb), $^{185}$Pb was produced as a side product via the $2n$ channel. Cross sections of $\approx 110 \mu b$ and $\approx 30 \mu b$, respectively, were deduced for the $13/2^+$ α-decaying state. During both experiments the beam intensity was limited to $\approx 6$ pNA by the counting rates of the γ-ray detectors at the target area, resulting in total counting rates of $\approx 250$ Hz at the focal-plane implantation detector. The α-decay half-life, energy, and branching ratio measured earlier for the excited $13/2^+$ state in $^{185}$Pb are $4.3 \pm 0.1$ s, 6408 keV, and $50\%$, respectively [32].

Prompt γ rays were detected using the JUROGAM Ge detector array consisting of 43 Compton-suppressed single-crystal Ge detectors. The total photo-peak efficiency of this array for 1332 keV γ rays is 4.2%. The recoiling fusion-evaporation residues were separated in-flight from the beam using the gas-filled recoil separator RITU and implanted into a pair of double-sided silicon strip detectors (DSSSDs) of the GREAT focal-plane detection system [33]. In the DSSSDs, the energy of implanted recoils and their subsequent α decay were measured. Upstream of the DSSSDs, a multiwire proportional counter was used to extract energy loss of recoils and together with the DSSSD it allowed time-of-flight information to be deduced.

The energies of events occurring in all detectors were recorded by the triggerless total data readout data acquisition system and time-stamped using a 100-MHz clock [34]. Subsequent temporal and spatial correlations between the various detector groups were performed using the GRAIN data analysis package [35]. The high granularity of the DSSSDs (4800 pixels) enabled the RDT method to be used for $^{185}$Pb, where the half-life of the α-decaying state is of the order of 5 s.

Prompt γ rays detected in coincidence with an implanted recoil followed by a subsequent $^{185}$Pb α decay in the same DSSSD pixel within 13 s were selected in the data analysis. The analysis of the data was completed with the RADWARE software package [36].

In Fig. 1, the α-particle energy spectra correlated with implanted recoils from both experiments are shown. Variations arise from the slightly different reactions. During 300 h of effective beam time, a total of $10^5$ events associated with the α decay of the $13/2^+$ isomeric state in $^{185}$Pb were recorded. Due to the fragmented decay structure and overlapping α-decay energies with $^{186}$Pb, the decay of the $3/2^-$ state could not be employed for RDT $\gamma \gamma$-coincidence analysis. Thus the present work concentrates only on the RDT study of the $13/2^+$ isomeric state.

Figure 2(a) shows the recoil-gated singles γ-ray energy spectrum correlated with the α decay of the $13/2^+$ state in $^{185}$Pb. The strongest transitions can be firmly assigned to $^{185}$Pb, but the existence of contaminant transitions originating from $^{185}$Tl, $^{182}$Hg, and $^{184}$Hg nuclei produced via $y p-x n$ and $\alpha-x n$ fusion-evaporation channels is apparent. This contamination arises from random correlations with recoils implanted into the same pixel of the DSSSD between implantation and

![Fig. 1. Energy spectra of α particles measured in the DSSSDs of the GREAT spectrometer correlated with implanted recoils within a search time of 13 s. The spectrum (a) is from the $^{82}$Kr + $^{106}$Pd reactions and spectrum (b) from the $^{83}$Kr + $^{104}$Pd reactions. The shaded areas correspond to energy gates used for tagging and the energy range between 6250 and 6800 keV has been magnified (by factor of 5) for illustration purposes.](image1)

![Fig. 2. (a) Singles γ-ray energy spectrum gated with recoils and tagged with α decays of the $13/2^+$ state in $^{185}$Pb. (b), (c), and (d) Recoil-gated, α-tagged γγ coincidence spectra with a gate on the 817-, 242-, and 373-keV transitions, respectively. Transitions associated with $^{185}$Pb are labeled with energies, whereas contaminant transitions are marked with *, o, and x for $^{185}$Tl, $^{182}$Hg, and $^{184}$Hg, respectively.](image2)
TABLE I. The γ-ray transitions measured in the present γ-ray energy, relative γ-ray intensity, and tentatively assigned spins are listed.

<table>
<thead>
<tr>
<th>Eγ (keV)</th>
<th>Irel</th>
<th>Iγ → Iγ</th>
</tr>
</thead>
<tbody>
<tr>
<td>151.8(3)</td>
<td>15(3)</td>
<td>–</td>
</tr>
<tr>
<td>242.0(3)</td>
<td>39(5)</td>
<td>(19/2+ → 17/2+)</td>
</tr>
<tr>
<td>301.4(4)</td>
<td>12(3)</td>
<td>(23/2+ → 21/2+)</td>
</tr>
<tr>
<td>344(1)</td>
<td>15(10)</td>
<td>(19/2+ → 15/2+)</td>
</tr>
<tr>
<td>344.2(3)</td>
<td>36(10)</td>
<td>(17/2+ → 13/2+)</td>
</tr>
<tr>
<td>370(1)</td>
<td>&lt;10</td>
<td>–</td>
</tr>
<tr>
<td>372.8(3)</td>
<td>60(7)</td>
<td>(21/2+ → 17/2+)</td>
</tr>
<tr>
<td>432.1(3)</td>
<td>76(9)</td>
<td>(23/2+ → 19/2+)</td>
</tr>
<tr>
<td>445.8(3)</td>
<td>61(8)</td>
<td>(25/2+ → 21/2+)</td>
</tr>
<tr>
<td>473.9(3)</td>
<td>73(9)</td>
<td>(13/2+ → 13/2+)</td>
</tr>
<tr>
<td>509.7(6)</td>
<td>26(6)</td>
<td>(27/2+ → 23/2+)</td>
</tr>
<tr>
<td>715.4(6)</td>
<td>24(5)</td>
<td>(15/2+ → 13/2+)</td>
</tr>
<tr>
<td>817.3(6)</td>
<td>100(10)</td>
<td>(17/2+ → 13/2+)</td>
</tr>
<tr>
<td>1002(2)</td>
<td>16(5)</td>
<td>–</td>
</tr>
</tbody>
</table>

The coincidence relation between the 817-keV transition and the transitions at 242 and 373 keV is confirmed in the spectra shown in Figs. 2(c) and 2(d). They also prove that the 242- and 373-keV transitions do not form a cascade. Thus, they are set to feed the 17/2+ state and their parent states are assigned as 19/2+ and 21/2+, respectively.

Another common feature in the spectra shown in Figs. 2(c) and 2(d) are the transitions at 344 and 474 keV, which are in mutual coincidence and sum up to 818 keV. Because they do not coincide with the 817-keV transition, they are considered an alternative de-excitation path for the 818-keV state. The ordering of this cascade is deduced on the basis of intensity balance arguments. The 474-keV state is assigned as 13/2+. The assignment is also supported by the non-observation of the 586- and 1060-keV transitions (which would have multipole order higher than 2) from the 19/2+ state.

The transitions feeding the 19/2+ and 21/2+ states can be seen in Figs. 2(c) and 2(d). The 432- and 510-keV transitions form a cascade feeding the 19/2+ state, whereas the 446-keV transition populates the 21/2+ state. Other transitions, not discussed here, were placed into the level scheme based on similar considerations. The isomeric α decaying 13/2+ state in 185Pb presumably represents a coupling of the i13/2 quasineutron to the spherical ground state of the even-mass Pb core [32].

The level scheme above the 474-keV 13/2+ state clearly resembles a strongly coupled rotational band with E2 cascades above the 13/2+ and 15/2+ states connecting levels of favored and unfavored signatures, respectively. The non-observation of transitions from favored to unfavored states can be explained by relatively large internal conversion due to small transition energies.

A quadrupole deformation parameter β2 = 0.29 is extracted from the lifetime measurements for the suggested prolate yrast band in 186Pb [17]. The oblate band is expected to represent a less deformed shape of β2 ~ -0.15 [8,15]. Within the framework of the Nilsson model, both at the prolate and oblate side, the odd neutron occupies the i15/2 [633] (or f9/2 [624]) orbital of i13/2 origin. It can be expected that coupling of this neutron to a prolate core results in a strongly coupled band,
and is also in accord with the value deduced for $^{185}\text{Hg}$ shown relative to the $^{13}$In.

In the odd-mass isotopes, the level energies of favored states are observed band structure in $^{185}\text{Pb}$ and the strongly coupled is supported by the level scheme of Fig. 3. Whereas coupling to a less-deformed oblate core may lead to a decoupled band structure [28]. The strong coupling scheme is supported by the level scheme of Fig. 3.

In fact, there are remarkable similarities between the observed band structure in $^{185}\text{Pb}$ and the strongly coupled prolate bands seen in Hg and Pt isotopes in the vicinity of the $^{15}$Iπ = 10/2 level. The value is roughly consistent with the corresponding value in $^{181}\text{Pt}$ (0.14(2)$\mu^2_N/e^2b^2$) [39] and is also in accord with the value deduced for $^{185}\text{Hg}$ ($\approx 0.1\mu^2_N/e^2b^2$) [38].

The band in $^{181}\text{Pt}$ shown in Fig. 4 has been associated with the $^9\pi_2$ [624] Nilsson orbital and is seen down to the $9/2^+$ level. In $^{185}\text{Pb}$ such non-yrast levels below the $13/2^+$ level may well be bypassed by high-energy transitions to the $13/2^+$ state. The signature splitting in these bands in $^{185}\text{Pb}$ and $^{181}\text{Pt}$ are similar. In Ref. [39] it is associated with admixture of a low-$\Omega$ component or with triaxiality.

The present data show that in $^{185}\text{Pb}$ the $\mathcal{B}(E2; 17/2_1^+ \rightarrow 13/2_2^+)$ strength is approximately 30 times higher than for the $17/2_2^+ \rightarrow 13/2_2^+$ transition supporting suggestion that the $13/2_2^+$ state is a member of the prolate band. Compared to the similar band in the isotope $^{181}\text{Pt}$, the energy of the $13/2_2^+$ state is lower than that expected from the regular rotational band structure. This lowering could be due to mixing with the (unobserved) oblate $13/2^+$ state.

In Fig. 5 systematics of some yrast levels in neutron deficient Pb isotopes are shown. The near-degeneracy of level energies between the even- and odd-$A$ Pb isotopes for $A \geq 191$ reveals the weak coupling of the $i_{13/2}$ quasineutron to a spherical core [21–25]. In isotopes with $A \leq 189$ this degeneracy is broken as the yrast $17/2^+$, $21/2^+$, and $25/2^+$ levels lie higher than the yrast $2^+$, $4^+$, and $6^+$ levels, respectively, which is typical of a change toward a strong coupling scheme [53].

As discussed in the introduction, possible strongly coupled structures have been observed in $^{185}\text{Pb}$ and $^{187}\text{Pb}$, though the band in $^{187}\text{Pb}$ could also be interpreted as weak coupling of the $i_{13/2}$ quasineutron. The strongly coupled picture is supported by the present observation of the prolate band in $^{185}\text{Pb}$. It should be noted that a 472-keV $13/2^+_2$ state in $^{187}\text{Pb}$ is seen in the $\alpha$-decay study by Andreyev et al. and associated with the prolate shape [54].

In summary, excited states in $^{185}\text{Pb}$ have been observed for the first time in RDT in-beam $\gamma$-ray measurements and a tentative level scheme above the $13/2^+$ isomeric state has been established. The structure for states above spin $15/2$ is suggested to be a strongly coupled band based on the $^9\pi_2$ [624] orbital, similar to that described by Baxter et al. [20]. The level energy of the $13/2^+_2$ state is lower than that expected from the observed band, suggesting the presence of the close-lying (unobserved) oblate $13/2^+$ state. Consequently, the present data provide direct evidence for prolate deformation in Pb isotopes near the $N = 104$ neutron midshell.

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