Cascaded third harmonic generation in lithium niobate nanowaveguides
Alexander S. Solntsev, Andrey A. Sukhorukov, Dragomir N. Neshev, Rumen Iliev, Reinhard Geiss, Thomas Pertsch, and Yuri S. Kivshar

Citation: Applied Physics Letters 98, 231110 (2011); doi: 10.1063/1.3597627
View online: http://dx.doi.org/10.1063/1.3597627
View Table of Contents: http://scitation.aip.org/content/aip/journal/apl/98/23?ver-pdfcov
Published by the AIP Publishing

Articles you may be interested in
Second harmonic generation in phase matched aluminum nitride waveguides and micro-ring resonators

Continuous-wave cascaded-harmonic generation and multi-photon Raman lasing in lithium niobate whispering-gallery resonators

Second-harmonic generation in periodically poled lithium niobate waveguides fabricated by femtosecond laser pulses

First-order quasi-phase-matched blue light generation in surface-poled Ti:indiffused lithium niobate waveguides
Appl. Phys. Lett. 84, 4430 (2004); 10.1063/1.1758776

Wavelength shifting of optical pulses through cascaded second-order processes in a lithium–niobate channel waveguide
Appl. Phys. Lett. 75, 1198 (1999); 10.1063/1.124640

This article is copyrighted as indicated in the article. Reuse of AIP content is subject to the terms at: http://scitation.aip.org/termsconditions. Downloaded to IP: 150.203.176.45 On: Fri, 20 Jun 2014 00:40:58
Cascaded third harmonic generation in lithium niobate nanowaveguides

Alexander S. Solntsev,1,a) Andrey A. Sukhorukov,1 Dragomir N. Neshev,1 Rumen Iliev,2 Reinhard Geiss,3 Thomas Pertsch,3 and Yuri S. Kivshar1
1Nonlinear Physics Centre and Centre for Ultra-high bandwidth Devices for Optical Systems (CUDOS), Research School of Physics and Engineering, Australian National University, Canberra ACT 0200, Australia
2Institute of Condensed Matter Theory and Solid State Optics, Friedrich-Schiller-Universität Jena, Max-Wien-Platz 1, 07743 Jena, Germany
3Institute of Applied Physics, Friedrich-Schiller-Universität Jena, Max-Wien-Platz 1, 07743 Jena, Germany

(Received 27 March 2011; accepted 12 May 2011; published online 9 June 2011)

We predict highly efficient third harmonic generation through simultaneous phase-matching of second-harmonic generation and sum-frequency generation in lithium niobate nanowaveguides, enabled due to strong modal dispersion. We demonstrate that the waveguide size which corresponds to phase-matching is also optimal for highest mode confinement and therefore for strongly enhanced conversion efficiency. © 2011 American Institute of Physics. [doi:10.1063/1.3597627]

Parametric frequency conversion and harmonic generation are among the most intensively studied phenomena in nonlinear optics. It was demonstrated that important advantages can be obtained by cascading several parametric processes.1 In particular, the highest efficiency third harmonic generation (THG) can be achieved in media with quadratic nonlinearity through two cascaded parametric processes: (i) second harmonic generation (SHG) and (ii) sum-frequency generation (SFG) that incorporates mixing of the fundamental wave (FW) and the second harmonic (SH) to generate the third harmonic (TH). The conversion is most efficient when the phase-matching (PM) conditions for both processes are satisfied.

Whereas material birefringence can be conveniently used to phase-match a single process,2 the simultaneous PM of cascaded processes requires engineering of linear or nonlinear material properties at microscale and nanoscale. In particular, quasi-PM (Ref. 3) of cascaded THG (Refs. 4 and 5) can be realized by dual-period inversion of the crystal domain structure through electric field poling of the crystal.

With the development of nanotechnology, it became possible to fabricate high-index-contrast nanowaveguides which provide strong spatial confinement of the guided modes thus enhancing the nonlinear interactions. By using such waveguides one can achieve PM of quadratic nonlinear processes through dispersion engineering of guided modes.6–10 This is a flexible approach that avoids the need for additional periodic poling of the waveguide and has been widely used for PM of four-wave mixing nonlinear interactions.11

In this letter, we predict that ultrathin LiNbO3 waveguides suspended in air can be used for efficient cascaded THG. Air suspended LiNbO3 slab waveguides were shown to be feasible for fabrication at various thicknesses12,13 and with higher quality in comparison to epitaxially grown LiNbO3 films.14 The SHG in LiNbO3 material was studied theoretically in photonic crystals10 and thin films on a substrate.7 Furthermore efficient SHG was also predicted for AlGaAs slot waveguides,6 rods,8 and thin high-index-contrast AlGaAs/oxidized AlAs waveguides.9 However, the simultaneous PM of cascaded parametric processes in nanowaveguides has never been considered. We predict that complete PM of both cascaded quadratic processes can be realized simultaneously in a single waveguide without periodic poling. The high quadratic nonlinearity of LiNbO3 and tight field confinement in a nanowaveguide can allow for a strong enhancement of the conversion efficiency in comparison to quasiphase-matched cascaded THG in periodically poled LiNbO3 waveguides15 and direct THG through cubic nonlinearity in silica glass waveguides.16

To get a better insight in the possibilities for PM of the cascaded THG, we first develop a semi-analytical model that describes PM in LiNbO3 slab waveguides. We then show that this model can also be used as a starting point to design more practical nanowire waveguides. For efficient frequency conversion, in addition to PM, it is desirable to employ nonlinear interactions based on the largest nonlinear susceptibility tensor components. We, therefore, perform a systematic analysis of different slab orientations, and find that the most efficient cascaded THG is realized in a z-cut LiNbO3 slab waveguide with all interacting waves propagating in y direction, as illustrated in Fig. 1(a).

We determine that the optimal THG process in the LiNbO3 slab waveguide is the conversion of FW TE0 mode into SH TM0 mode, and then their mixing to the TH TE1 mode in the process of SFG [see Fig. 1(b)]. The electric field profiles of the guided modes can be expressed as E = exp[−iωt + ik0π(z, ω)] × [E0(z, ω), E0(z, ω), E0(z, ω)], where n eff is the effective mode index, ω is the fundamental optical frequency, k0 = ω/c, and c is the speed of light in vacuum. For TE modes, the electric field is polarized in the x direction (Ez = 0), and the electric field component Ex satisfies the wave equation: ∇2Ex/ν2 = 2Ezn eff [n eff (ν eff)2 − n2], where n x,z are refractive index components, equal to those of congruent LiNbO3 (Ref. 16) for |z| ≤ h/2 (inside the slab waveguide), and n x,z = 1 for |z| > h/2 (outside the slab waveguide), where h is the waveguide thickness. For TM modes, the electric field is polarized in the y-z plane and can be expressed through the single component of the magnetic field Hx, Ex = −2πfHx n eff n y/z Hx /ν eff with the vacuum impedance Z0 = (μ0/ε0)1/2. The wave equation for the magnetic field is n z2 ∇2 n y/z ∇ Hx /ν eff = Hx k0 [n eff (ν eff)2 − n2].

a)Electronic mail: sun124@physics.anu.edu.au
The normalized effective coefficients for SHG and SFG in the undepleted narrow band pump approximation can be defined as $\eta_{\text{SHG}} = \gamma_{\text{SHG}}^2$ and $\eta_{\text{SFG}} = \gamma_{\text{SFG}}^2$. We estimate these efficiencies for the beam width equal to 1.77 μm in x direction (for the later comparison with fully vectorial calculation for nanowire waveguides): $\eta_{\text{SHG}} = 347\% \ W^{-1} \ cm^{-2}$, $\eta_{\text{SFG}} = 215\% \ W^{-1} \ cm^{-2}$. Total normalized conversion efficiency for phase-matched THG in a waveguide length $L$ can be defined as $\eta_{\text{THG}} = \gamma_{\text{THG}}^2 |W(L)|^2/|U|^2 = \eta_{\text{SHG}} \eta_{\text{SFG}} |U|^2 L^2/4$. It is most remarkable that the slab waveguide thickness of $h = 206 \text{ nm}$ also corresponds to the strongest mode confinement and therefore to the highest nonlinear coefficient for THG, as shown in Fig. 1(d).

We find that both PM conditions can be satisfied for different FW wavelengths by manufacturing a slab waveguide with appropriate thickness and by heating or cooling the sample, see Fig. 2. Furthermore, it is possible to engineer the ratio $\gamma_{\text{SHG}}/\gamma_{\text{SFG}}$, which can enable nearly complete conversion of energy into TH.\(^{18}\)

We now consider a nanowire waveguide with rectangular cross-section [see Fig. 3(a)], in which higher conversion efficiency can be achieved due to mode confinement in both transverse dimensions (z, x). We calculate numerically the FW, SH, and TH modes in nanowaveguides with a rectangular cross-section using the COMSOL rf module. We start with crystal orientation and waveguide thickness $h$ as in the slab waveguide analysis and then optimize the FW frequency and

---

**FIG. 1.** (Color online) (a) LiNbO$_3$ slab waveguide orientation for THG. (b) Electric field profiles for slab waveguide thickness of 200 nm and FW wavelength of 1542 nm. (c) Effective refractive index vs slab waveguide thickness for FW, SH, and TH modes. (d) Normalized square of THG nonlinear coefficient for slab waveguide.

---

**FIG. 2.** (Color online) The slab waveguide thickness (solid line, left axis) and temperature (dashed line, right axis) corresponding to exact PM for THG vs FW wavelength.

---

**FIG. 3.** (Color online) (a) Scheme of the air-suspended LiNbO$_3$ waveguide. [(b)-(d)] Intensity profiles of phase-matched (b) FW, (c) SH, (d) TH waves for a waveguide width $b = 1.77 \mu m$ and thickness $h = 181 \text{ nm}$. (e) FW wavelength $\lambda_{\text{FW}}$ and (f) the waveguide thickness $h$ corresponding to exact PM for THG vs waveguide width $b$.
waveguide thickness to achieve complete PM. Characteristic modes of the interacting FW, SH, and TH waves in the waveguide are shown in Figs. 3(b)–3(d). We demonstrate in Figs. 3(e) and 3(f) that by varying the waveguide width $b$, we can satisfy the conditions for fully phase-matched THG for pump wavelengths between 1.35 and 1.55 μm. Using the calculated mode profiles we obtain the effective areas and the conversion efficiency for the cascaded THG. For $\lambda_{FW}=1471$ nm, a waveguide of width $b=1.77$ μm and thickness $h=181$ nm, the effective areas are $A_{SHG}=22$ μm$^2$ and $A_{SFG}=26$ μm$^2$. This corresponds to normalized conversion efficiencies $\eta_{SHG}=261\% \ W^{-1} \ cm^{-2}$, $\eta_{SFG}=279\% \ W^{-1} \ cm^{-2}$. We note that these values agree well with our previous estimates based on semianalytical analysis for a slab waveguide. Total THG conversion efficiency $\eta_{THG}$ is sufficiently high to predict, in an ideal waveguide with a 3 mm interaction length, the generation of 1 mW green light from 33 mW source at a telecommunication wavelength. To compare with the best result reported to date, such TH output from ideal periodically poled LiNbO$_3$ structure is predicted to require ten times longer crystal and almost four times higher pump power.$^5$

The realization of LiNbO$_3$ nanowaveguides with the desired geometry is feasible by means of ion-beam enhanced etching (IBEE). The IBEE technology has been shown to be ideally suited for the fabrication of complex photonic crystal structures$^{19,20}$ and can also be applied to fabricate the proposed nanowaveguides. In this process the geometry of a patterned masking layer is transferred into the crystal by a series of high energy ion irradiation. The irradiated and thus damaged regions are subsequently removed by chemical wet etching, resulting in an air-bridged structure, as shown schematically in Fig. 3(a). We note that complete PM requires high manufacture precision. The thickness of 100 μm long slab waveguides has to be controlled with nanometer accuracy, which may be challenging with technologies currently available. Nevertheless, THG may be realized even when the individual SHG and SFG processes are slightly mismatched, provided that a single PM condition between the FW and TH waves is satisfied.$^1$ We anticipate that broadband THG may be possible in the latter case, although at the trade-off of lower conversion efficiency.

In conclusion, we have shown that the modal dispersion in air-suspended lithium niobate waveguides can be used to simultaneously phase-match two different nonlinear parametric processes, resulting in cascaded THG. We anticipate that our findings may stimulate the realization of distinct families of efficient frequency mixers and converters to the TH, for applications in compact light sources and laser display technologies.

We acknowledge the support by the Australian Research Council, the Australian Academy of Science, Australian National Computational Infrastructure, and German Research Foundation, Grant No. NanoGuide, PE 1524/5-1.